

Marks : 100	PART – II (CLASS-XII)	Time: 3 Hours
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UNIT-1 FUNCTIONS AND LIMITS**Introduction**

Concept of Function, Definition (Function – Domain – Range), Notation and Value of a Function, Graphs of Algebraic Functions, Graph of Functions Defined Piece-wise.

Types of Functions

Algebraic Functions, Trigonometric Function, Inverse Trigonometric Functions, Exponential Function, Logarithmic Function, Hyperbolic Functions, Inverse Hyperbolic Functions, Explicit Function, Implicit Function, Even Function, Odd Function

Composition of Functions and Inverse of a Function

Composition of Functions, Inverse of a Function, Algebraic Method to find the Inverse Function

Limit of a Function and Theorems on Limits

Meaning of the Phrase “x approaches zero”, Meaning of the Phrase “x approaches infinity”, Meaning of the Phrase “x approaches a”, Concept of Limit of a Function, Limit of a Function, Theorems on Limits of Function

Limits of Important Functions

$\lim_{x \rightarrow a} \frac{x^n - a^n}{x - a} = na^{n-1}$ where n is an integer and $a > 0$, $\lim_{x \rightarrow 0} \frac{\sqrt{x+a} - \sqrt{a}}{x} = \frac{1}{2\sqrt{a}}$ Limit at Infinity,

Method for Evaluating the Limits at Infinity, $\lim_{x \rightarrow +\infty} \left[1 + \frac{1}{n}\right] = e$, $\lim_{x \rightarrow 0} \frac{a^x - 1}{x} = \log_e a$ The

Sandwich Theorem, If θ is measured in radian, then $\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$.

Continuous and Discontinuous Functions

One-Sided Limits, Criterion for Existence of Limit of a Function, Continuity of a function at a number

Graphs

Graph of the Exponential Function $f(x) = a^x$, Graph of the Exponential Function $f(x) = e^x$, Graph of Common Logarithmic Function $f(x) = \lg x$, Graphs of Natural Logarithmic Function $f(x) = \ln x$, Graphs of Implicit Functions, Graph of Parametric Equations, Graphs of Discontinuous Functions, Graphical Solution of the Equation

UNIT-2 DIFFERENTIATION : Introduction

Average Rate of Change, Derivative of a Function

Finding $f'(x)$ from definition of derivative

Derivation of x^n where $n \in \mathbb{Z}$, Differentiation of Expressions of the Types

Theorems on Differentiation**The chain rule****Derivatives of inverse functions****Derivative of a Function given in the form of parametric equations****Differentiation of Implicit Relations****Derivatives of Trigonometric Functions****Derivatives of inverse Trigonometric functions****Derivative of exponential functions****Derivative of the logarithmic function****Logarithmic differentiation****Derivative of Hyperbolic functions****Derivatives of the inverse hyperbolic functions****Successive Differentiation (or Higher derivatives)****Series expansions of functions****Taylor series expansions of functions****Geometrical interpretation of a derivative****Increasing and decreasing functions****Relative extrema****Critical values and critical points****UNIT-3 INTEGRATION: Introduction**

Differentials of Variables, Distinguishing between dy and δy ,

Finding $\frac{dy}{dx}$ by using differentials, Simple application of differentials

Integration as anti-derivative (Inverse of derivative)

Some Standard Formulae for Anti-Derivatives, Theorems on Anti-Derivatives, Anti-Derivatives of $[f(x)]^n f'(x)$ and $[f(x)]^{-1} f'(x)$.

Integration by method of substitution**Some useful substitutions****Integration by parts****Integration involving partial fractions****The definite integrals**

The area Under the curve, Fundamental theorem and properties of Definite Integrals

Application of definite integrals**Differential equations**

Solution of a differential equation of first order, Initial conditions

UNIT-4 INTRODUCTION TO ANALYTIC GEOMETRY: Introduction

The Distance Formula, Point dividing the join of two points in a given ratio

Translation and rotation of axes**Equations of straight lines**

Slope or gradient of a straight line joining two points, Equation of a straight line parallel to the x-axis (or perpendicular to the y-axis), Equation of a straight line parallel to the y-axis (or perpendicular to the x-axis), Derivation of standard forms of equations of straight lines, A linear equation in two variables represents a straight line, To transform the general linear equation to standard forms, Position of a point with respect to a line

Two and three straight lines

The Point of intersection of two Straight Lines, Condition of concurrency of three Straight Lines, Equation of Lines through the Point of Intersection of Two Lines, Distance of a Point from a Line, Distance between two Parallel Lines, Area of a Triangular region whose vertices are given

Angle between two lines

Equation of a straight line in Matrix form

Homogeneous equation of the second degree in two variables

Homogeneous Equation, To find measure of the Angle between the Lines represented by $ax^2 + 2hxy + by^2 = 0$

UNIT-5 LINEAR INEQUALITIES AND LINEAR PROGRAMMING: Introduction**Linear Inequalities**

Graphing of a linear inequality in two variables

Region bounded by 2 or 3 simultaneous Inequalities**Problem Constraints****Feasible solution set****Linear Programming****Linear Programming Problems****UNIT-6 CONIC SECTION: Introduction**

Equation of a Circle, General form of an Equation of a Circle, Equations of Circles determined by given conditions

Tangents and Normals

Length of the Tangent to a Circle (Tangential Distance)

Analytic proofs of important Properties of a Circle**Parabola**

General form of an Equation of a Parabola, Other standard Parabolas, Graph of the Parabola

Ellipse and its Elements

Standard form of an Ellipse, Graph of an Ellipse

Hyperbola and its Elements

Standard equation of Hyperbola, Graph of the Hyperbola

Tangents and normals**Translation and Rotation of Axes****The General Equation of Second Degree**

Classification of conics by the discriminant

UNIT-7 VECTORS: Introduction

Geometric interpretation of Vector, Multiplication of Vector by a Scalar, Addition and Subtraction of two Vectors, Position Vector, Vectors in a plane, Properties of magnitude of a Vector, Another notation for representing vector in plane. A unit Vector in the direction of another given Vector, The ratio formula, Vector Geometry

Introduction of Vector in Space

Concept of a vector in space, properties of Vectors, Another notation for representing Vectors in space, Distance between two points in space, Direction Angles and Direction Cosines of a Vector

The Scalar product of two Vectors

Deductions of the important results, Perpendicular (Orthogonal) Vectors, Properties of dot product, Analytical expression of dot product $\underline{u} \cdot \underline{v}$, Angle between two Vectors, Projection of one Vector upon another Vector

The cross product or vector product of two vectors

Derivation of useful results of cross products, Properties of cross product, Analytical Expression of $\underline{u} \times \underline{v}$, Parallel Vectors, Area of Parallelogram, Area of Triangle

Scalar Triple product of Vectors

Analytical expression of $\underline{u} \cdot (\underline{v} \times \underline{w})$, The volume of the Parallelepiped, The volume of the Tetrahedron, Application of Vectors in Physics and engineering.

TOPIC-WISE WEIGHTAGE & TIME (XII)

UNIT	TOPIC		WEIGHT AGE	PERIODS (45 minutes each)
I	Functions & limits		6%	11
II	Differentiation of Functions	Polynomial & Algebraic Trigonometry and Inverse Trigonometric Logarithmic & Exponential	15%	07 07 07
	Successive differentiation and theorems and Maximum/Minimum		5%	07
III	Integration (Indefinite Integrals)	Standard forms By partial fractions By Substitution	29%	07 07 05
	Definite Integrals	By parts Area under the curve Differential Equations		07 07
IV	Introduction to Analytic Geometry		8%	13
V	Linear In-Equalities Linear Programming		7%	07 05
VI	Conic Sections	Circle Parabola Ellipse Hyperbola General Equation	17%	12 04 04 04 04
VII	Vectors	Introduction to vector & Scalar Product Vector product Scalar triple Product	13%	07 07 04
			100%	150 (6 periods a week)

Recommended Book: "MATHEMATICS Part-II"

Author : 1. Prof. Muhammad Amin Chaudhary 2. Prof. Muhammad Sharif Ghauri
3. Prof. Muhammad Khalid Saleem 4. Mr. Mazhar Hayat

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